

Math 27, HW #11 Selected Problems

Pg. 110, #34  $f(x) = \frac{3x^7 - 2x^5 + 5x^3 + 6x^2}{(-4)}$

Degree = 7 (odd)      Leading coefficient =  $\frac{3}{4}$  (+)

End Behavior: Falls to left and Rises to the right.

Pg. 110, #48  $y = x^5 - 5x^3 + 4x$

a) Solve:  $0 = x^5 - 5x^3 + 4x$

$$0 = x(x^4 - 5x^2 + 4)$$

$$0 = x(x^2 - 1)(x^2 - 4)$$

Either  $x=0$  or  $x^2-1=0$  or  $x^2-4=0$

$$(x+1)(x-1)=0$$

$$x^2=4 \Rightarrow \sqrt{x^2} = \pm\sqrt{4}$$

$$x = -1 \quad x = 1$$

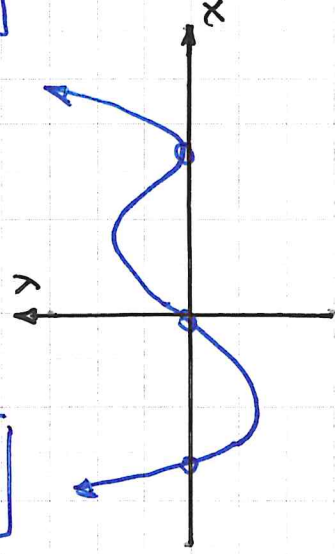
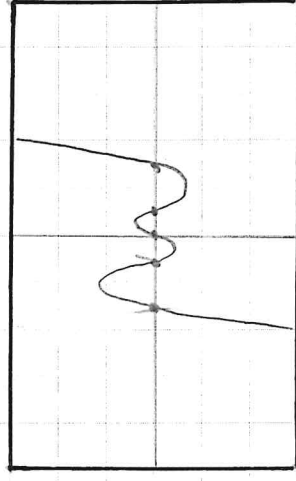
$$x = \pm 2$$

Pg. 110, #82

$$n = 4$$

$$a_4 > 0$$

3 real zeros



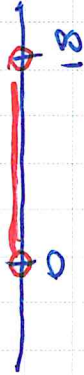
Pg. 111, #109

a) Volume = length  $\times$  width  $\times$  height

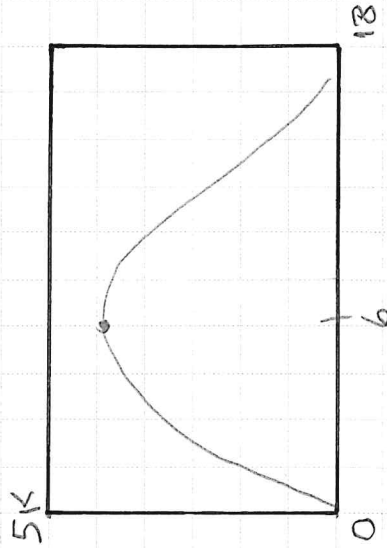
$$= (36 - 2x)(36 - 2x)x$$

$$= x(36 - 2x)^2$$

b) Domain of  $V$ :  $0 < x < 18$



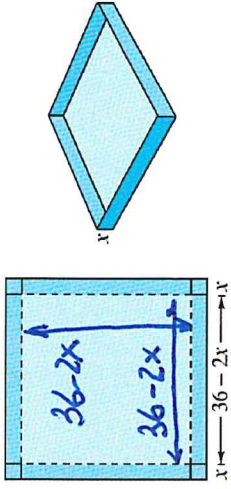
d)



$$\text{Max } V = 3,456 \text{ cm}^3$$

when  $x = 6 \text{ cm.}$

109. **Geometry** An open box is to be made from a square piece of material 36 centimeters on a side by cutting equal squares with sides of length  $x$  from the corners and turning up the sides (see figure).



(a) Verify that the volume of the box is given by the function  $V(x) = x(36 - 2x)^2$ .

(b) Determine the domain of the function  $V$ .

(d) Use the graphing utility to graph  $V$  and use the range of dimensions from part (c) to find the  $x$ -value for which  $V(x)$  is maximum.