

Pg. 67, #21  $f(x) = \sqrt{x-4}$  ;  $g(x) = x^2+4, x \geq 0$

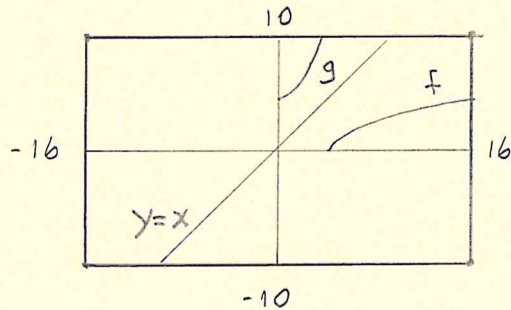
Note that:

$$(f \circ g)(x) = f(g(x)) = x$$

and that:

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So  $f$  and  $g$  are inverses.



Graphs are reflections in  $y=x$

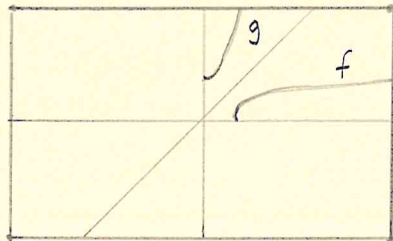
Pg. 67, #30  $f(x) = \sqrt[4]{3x-10}$  ;  $g(x) = \frac{x^4+10}{3}, x \geq 0$

a) Now,  $(f \circ g)(x) = f\left(\frac{x^4+10}{3}\right) = \sqrt[4]{3\left(\frac{x^4+10}{3}\right)-10} = \sqrt[4]{x^4} = x$

and  $(g \circ f)(x) = g\left(\sqrt[4]{3x-10}\right) = \frac{\left(\sqrt[4]{3x-10}\right)^4+10}{3} = \frac{3x}{3} = x$

Thus  $f$  and  $g$  are inverses.

b) Graph



Pg. 68, #42

The graph passes both the Vert. and Horiz. line tests

Thus, it is a one-to-one function.

Pg. 68, #74  $f(x) = x^3 + 1$

To find  $f^{-1}$ :

①  $y = x^3 + 1$

②  $x = y^3 + 1$

③  $x - 1 = y^3$

$$\sqrt[3]{x-1} = y$$

④  $f^{-1}(x) = \sqrt[3]{x-1}$

Graphs:

