

Math 1A
Test 1 - Extra Credit

Show all your work on engineering paper. NO CAS!

1. Evaluate the following limits. What does each limit tell you about functional behavior?
(1 point each)

a) $\lim_{x \rightarrow -3} \frac{x^3 + 27}{2x^2 + 7x + 3}$

b) $\lim_{x \rightarrow -4} \frac{x + 4}{1 - \sqrt{x + 5}}$

c) $\lim_{x \rightarrow -\infty} \frac{4x}{\sqrt{36x^2 + 3}}$

d) $\lim_{x \rightarrow 7^+} \frac{-x^2 + 5}{x^2 - 5x - 14}$

e) $\lim_{x \rightarrow +\infty} \left(\sqrt{9x^2 + 4x + 1} - 3x \right)$

2. Consider the functions below. Find all derivatives by using the short cut formulas.
(1 point each)

a) If $f(x) = \frac{Rx^3 - Sx^2 + T}{\sqrt{x}}$, find $f'(x)$.

b) Find $\frac{dy}{dx}|_{x=-1}$, where $y = 2\sqrt[3]{x} \cdot e^x$.

c) If $g(x) = \frac{f(x)}{4x^2 + 5x + 1}$ where $f(2) = -3$ and $f'(2) = 6$, find $g'(2)$.

d) If $H(t) = \frac{t^3 \cdot e^t}{1 + t^2}$, find $H'(t)$.

e) If $f(x) = \frac{-4\sqrt{x} + 6}{e^x}$, find $f'(4)$.